

# Advanced Macroeconomics – 9 May 2006

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- Inglise keele!
- 2.04 m.

## Today

- 11:15-12:15 + 12:45-14:00.
- Romer, ch. 10: Inflation
  - Skip section 10.6.
  - Skip p. 497-499 in section 10.7.
- Exercises → Toomas!

Overheads and whiteboard!

## Next Tuesday

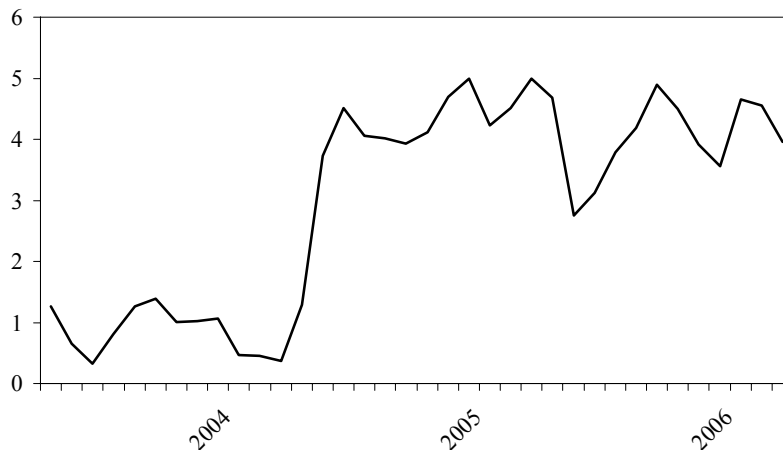
- Leftovers from ch. 10.
- Romer, ch. 11.

# Ch. 10: INFLATION AND MONETARY POLICY

Has Estonia an inflation problem?

- Is inflation a problem for Estonians?
- Maastricht criteria → Max average of 3 lowest + 1%.

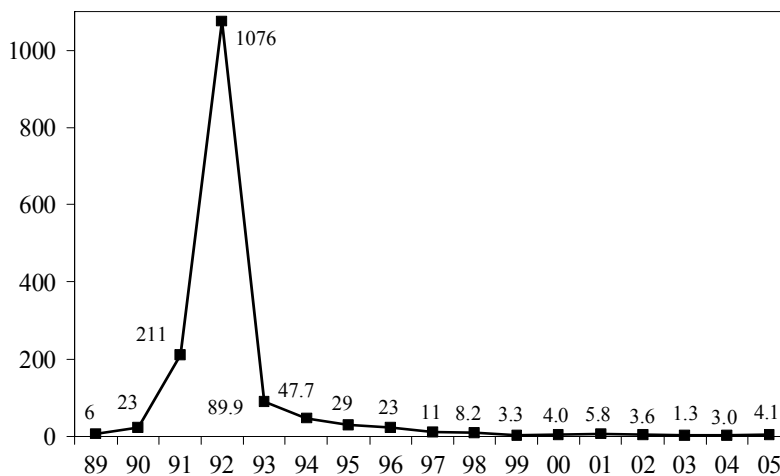
**Figure 1.** Consumer price inflation, month-on-month previous year, percent, April 2003 – March 2006



Sources: EBRD (various years), Statistical Office of Estonia

- Compare with past.

**Figure 2.** Consumer price inflation, percent per year



Sources: EBRD (various years), Statistical Office of Estonia

## 10.1 Introduction (p. 468-469)

Inflation = sustained increase in price level.

- General price level → not individual goods.
- Price jump ≠ inflation!

### “Types” of inflation

- Hyperinflation (Cagan:  $\pi > 50\%$  per month in 6 months).
- Extreme inflation ( $\pi >$  say 100% per year).
- Moderate inflation ( $\pi = 10\text{-}30\%$  per year & persistence).
- “Low inflation”?
- Relative → low vs. high?

Disinflation = reduction of inflation rate.

## Overview of inflation coverage

10.1 → Brief introduction.

10.9 → The costs of inflation.

### Explaining hyper- and extreme inflation

10.2 → Background: money and inflation.

10.8 → Explaining hyperinflation.

10.3 → Background: term structure.

### Explaining moderate and “low” inflation

5.4 (!) → The Phillips curve once again.

10.4-10.5 → Explaining low / moderate inflation [bias].

### Monetary policy

10.6 → Does policy matter? SKIP!

10.7 → Conduct of monetary policy.

### “Warning”

Ch. 10 → Inflation and monetary policy mainly in closed economy.

- Nothing on exchange rate policy, exchange rate bands, currency boards, currency unions, etc.
- Little on inertia / persistence, Balassa-Samuelson effect.

[Half picture ☹ / ☺.]

## 10.9 The Costs of Inflation (p. 519-524)

Inflation is costly! How costly?

- Economists → “nominal scaling” ⇒ costs moderate.
- USA → ☹, cf. “misery index”.
- Russia → ☹

“64 percent of Russians are most concerned about rising prices. [...] fewer than 1 percent said that their greatest concern is the limitation on human rights and democratic freedoms in Russia.” (VTsIOM / Interfax → RFE/RL NEWSLINE Vol. 5, No. 206, Part I, 30 October 2001.)

### Costs of anticipated (stable) inflation

- Shoe leather costs → Cost of non-interest bearing assets  
↑ ⇒ economise on cash (more visits to bank / less liquidity services of money).
- Menu costs → change nominal prices more often.
- Distort tax system → difficult index tax system.
- Nominal prices changed infrequently (even if indexed)  
⇒ steady inflation causes relative price variability.
- “Nominal blindness” ~ “money illusion” → more difficult to form expectations when future price changes.
  - NB: Stable anticipated 10% inflation of the kilometre.  
1 km = 1000 m, 1100 m, 1210 m, 1331 m, 1461.1 m ...
- Inflation as a signal about the ability / credibility of government. [Self-fulfilling expectations → Laar / Kallas]

## Costs of Variable Inflation

- Nominal contracts do not incorporate variable inflation  
⇒ real uncertainty ⇒ possible welfare loss.
  - Real wage uncertainty.
  - Real investment outcome uncertainty.

## Empirically

- High inflation negatively correlated with growth (e.g. in estimations for transition economies)
  - Causality, reverse causality or common factor behind?
- NB: Price jumps often correlated with output increases.

## Potential Benefits of Inflation

- If nominal wages downward rigid → inflation allows real wage fall (adjustment possibility).
- Nominal interest rates  $\geq 0$  → inflation implies real interest rates can be negative (expansive monetary policy).
- Inflation as revenue source for government (high inflation, low inflation).
- Irrational / uninformed agents might look at nominal wages: inflation ⇒ nominal wage growth ↑ → people 😊.

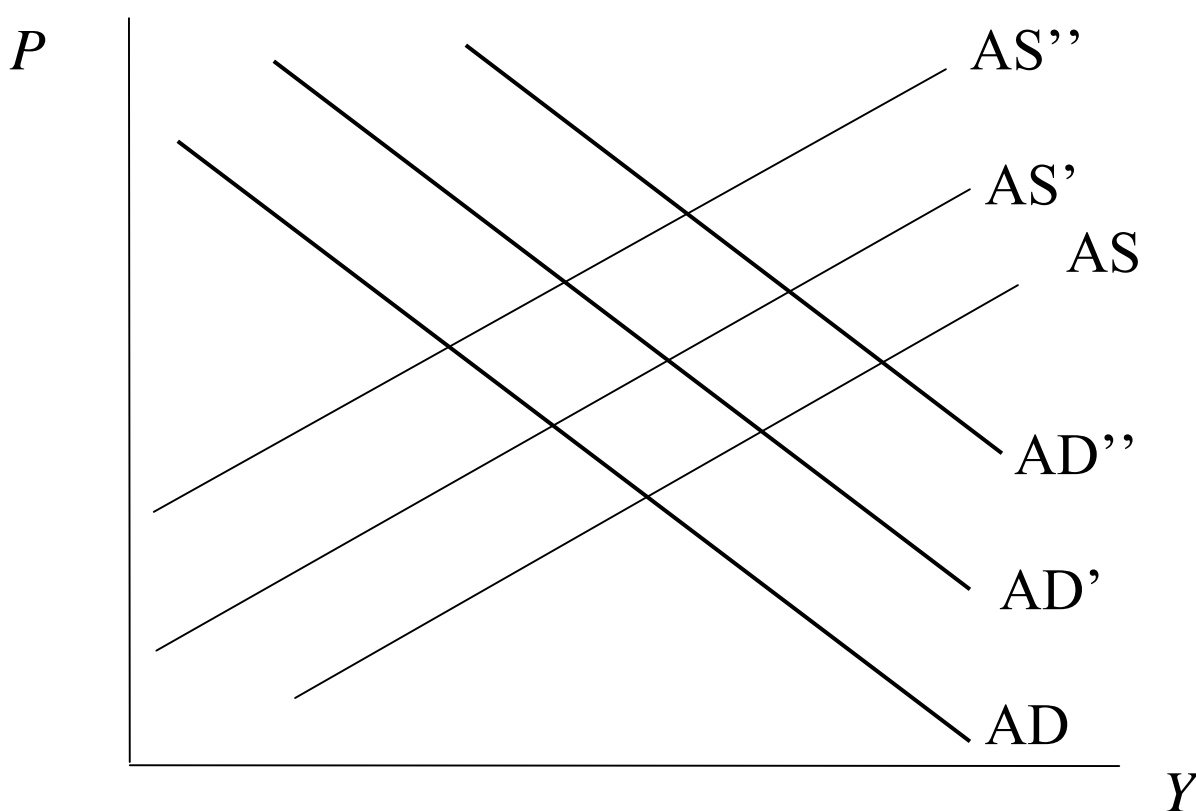
The “unfounded consensus” (p. 523-524) → Low inflation 😊, < 10% per year, better with 2% = “price stability”...

## 10.2 Inflation, Money Growth and Interest Rates (p. 469)

The “ultimate” cause of (high) inflation (1980s):

- Monetarists → money! → AD shocks
- Structuralists → structures / institutions! → AS shocks

AD-AS diagram

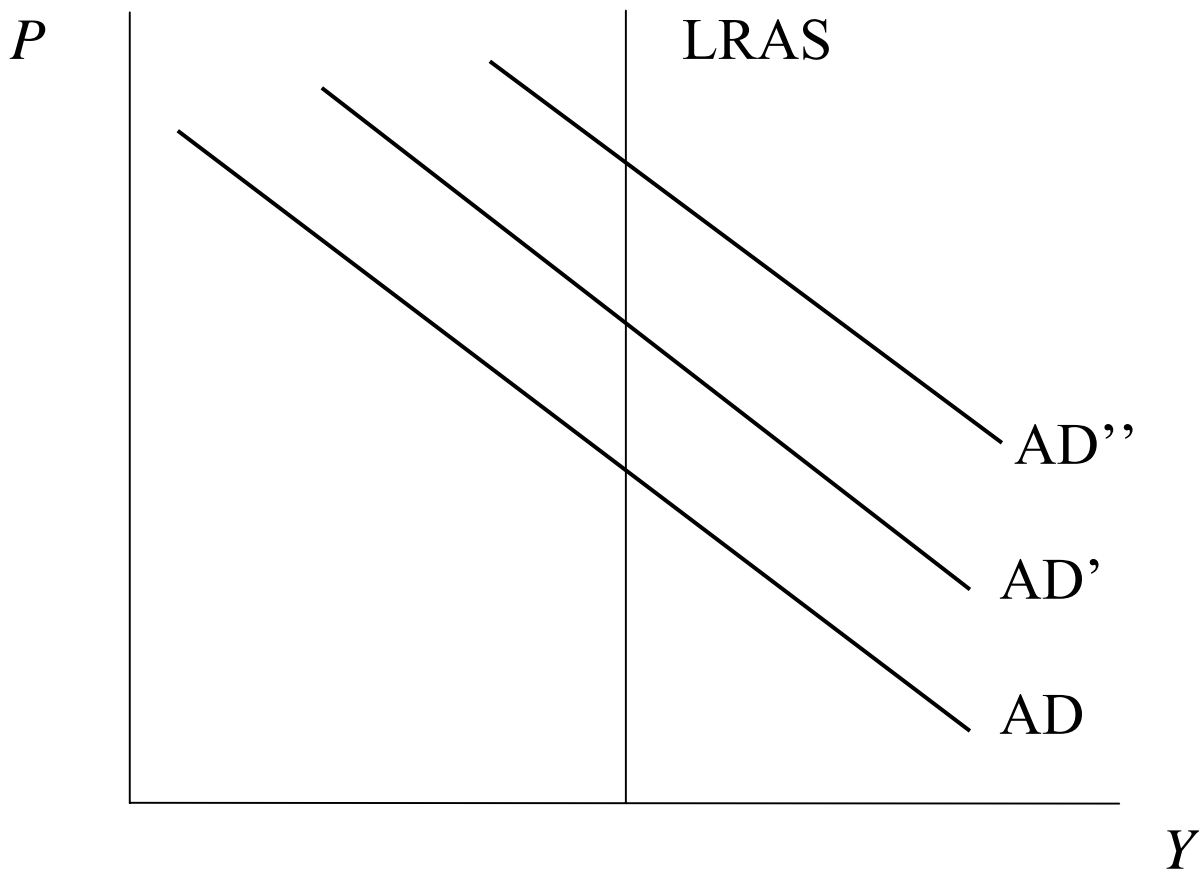


AS (e.g. bad productivity shocks) → not “forever” ☹

AD shocks (e.g.  $M \uparrow$ ) → long-term ☺

KAR: Convergence in views! → Institutions lead to excessive money issuance.

Long term  $\rightarrow$  AS curve vertical

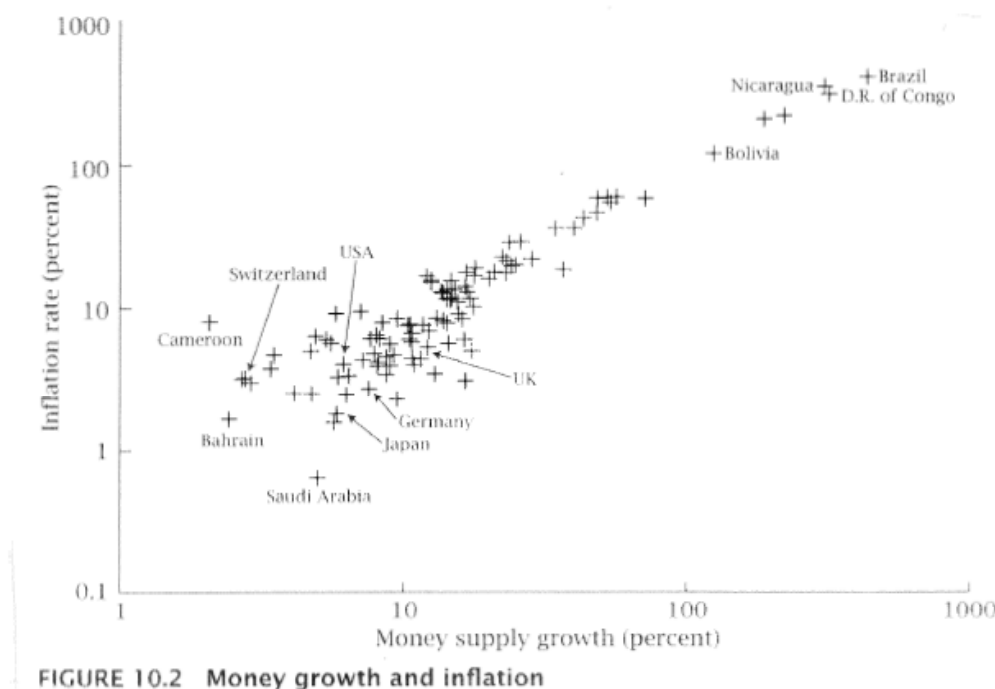


From derivation of AD curve  $\rightarrow$  money market equilibrium:

$$\frac{M}{P} = L(i, Y)$$
$$\Rightarrow$$
$$P = \frac{M}{L(i, Y)}$$

If nominal interest rate  $i$  and income  $Y$  constant  $\Rightarrow$  proportionality between  $M$  and  $P \Rightarrow$  growth rates correlated.

## 105 countries, 1980-95



- Inflation is a monetary phenomenon...
- ... at least if inflation is high
- ... at least in the longer term
- Individual country differences, mainly at low levels!

What about  $i$ ?

Ex post:  $r = i - \pi \Rightarrow i = r + \pi$ .

Ex ante: Fisher identity:  $i = r + \pi^e$ , where  $\pi^e$  = expected inflation.

- NB1: Fisher “identity”  $\rightarrow$  a “postulate”, e.g. no risk-premium.
- NB2: Quantity equation sometimes also called Fisher identity...

If Fisher equation holds and inflation  $\pi$  does not affect  $r$ , then Fisher effect:

$$\pi \uparrow \Rightarrow \pi^e \uparrow \Rightarrow i \uparrow \text{ (one-to one)}$$

## Disinflation with the Fisher effect

Assume  $\bar{r}$  and  $\bar{Y}$  constant  $\Rightarrow$

$$P = \frac{M}{L(\bar{r} + \pi^e, \bar{Y})}$$

Assume initial steady state  $\rightarrow \pi^e$  constant  $\Rightarrow P$  proportional to  $M \Rightarrow$

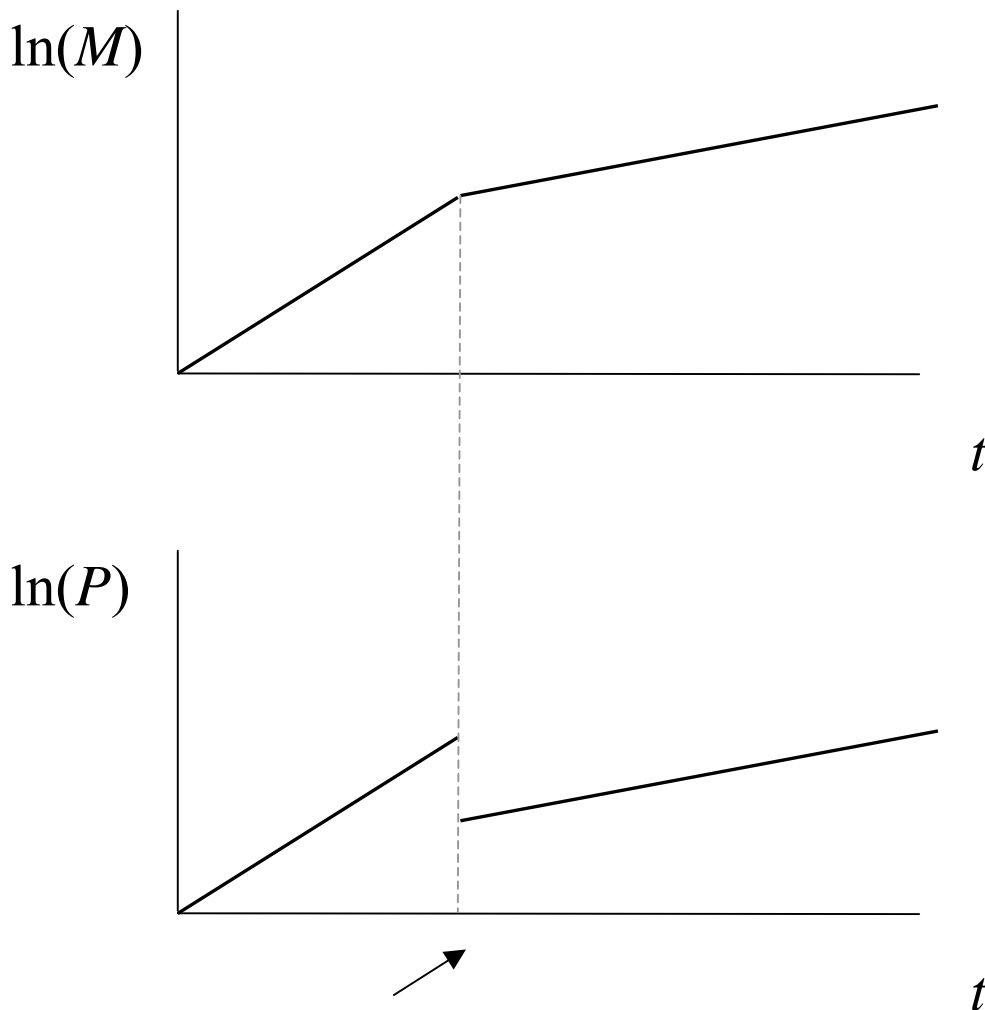
$$\pi = \frac{\dot{P}}{P} = \frac{\dot{M}}{M} = g_M$$

$\swarrow$   
 $= \pi^e$

[Often labelled  $\mu$ ]

Assume: Disinflation policy with  $g_M \downarrow$  announced.

- If believed / credible  $\Rightarrow \pi^e \downarrow$   
 $\Rightarrow$
- $L(\bar{r} + \pi^e, \bar{Y}) \uparrow$   
 $\Rightarrow$
- $P \downarrow$  (even before  $g_M \downarrow$ )



Lower  $g_M$  starts

“Real life problems” with money-based stabilisation

- Incentive to announce stabilisation (to attain price level dropping).
- Price  $\downarrow \Rightarrow$  real wage  $\uparrow \Rightarrow$  extra recessionary pressure.

Küsimus: How did Estonia disinflate in 1992?

## 10.8 Seignorage and Inflation (p. 510)

Explaining hyperinflation or extreme inflation.

- Why issue so much money?
- Model of money issuance...

Hyperinflation  $\rightarrow$  inflation  $\geq 50\%$  per month (for at least 6 months).

- $1.5^{12} \approx 129 = 12900\%$ .
- Hyperinflation  $\rightarrow$  always short periods.
- Germany: Jan. 1923 – Nov. 1923  $\rightarrow 2.6 \cdot 10^8$ .
- Hungary: Aug. 1945 – July 1946  $\rightarrow 10^{27}$ .
- Yugoslavia: Mid 1992 – mid 1993  $\rightarrow 10^{12}$ .

Extreme inflation  $\rightarrow$  inflation  $\approx 100\text{-}1000\%$  or  $5000\%$  per year.

- Latin America.
- Longer periods of time.

Explanation  $\rightarrow$  money growth! But why?

Money issuance as a way to finance government expenditures  $\rightarrow$  Seignorage = senioraaž, emissioonitulu.

... *Whiteboard (1)*

## 10.3 Monetary Policy and the Term Structure of Interest Rates (p. 474)

...*Whiteboard* (2)

### **EA: The Response of the Term Structure to Changes in the Federal Reserve's Federal-Funds-Rate Target (p. 476)**

Instrument of monetary policy in the USA → OMO operation on the Federal Funds (FF) market (overnight interbank rate).

- New York Fed → gold in basement, interventions on 12<sup>th</sup> floor!
- Küsimus: Interbank interest rates in EE?

Close correlation between FED's stated target rate and the FF rate ⇒ FF "exogenous".

Are long rates affected → term structure? [Cf. theory?]

$\Delta R_t^i$  = change in long-term interest rate (during  $i$ ).

$\Delta FF_t$  = change in  $FF$  (short-term) interest rate.

Estimations:

$$\Delta R_t^i = b_1^i + b_2^i \Delta FF_t + u_t^i$$

Results:

$$i = 3 \text{ months} \rightarrow b_2^i = 0.55$$

$$i = 1 \text{ year} \rightarrow b_2^i = 0.5$$

$$i = 5 \text{ year} \rightarrow b_2^i = 0.21$$

$$i = 20 \text{ year} \rightarrow b_2^i = 0.10$$

NB: Short-term interest rates positively correlated with long-term rates. ☹

- Explanation  $\rightarrow$  read rest of EA [other rates, premium]!

## 5.4 Output-Inflation Tradeoffs (p. 247-252)

The Phillips curve once again!

Equation (5.36), p. 248:

$$\pi_t = \pi_t^* + \lambda(\ln Y_t - \ln \bar{Y}_t) + \varepsilon_t^S$$

where  $\pi_t^*$  is “core inflation” or expected inflation.

Phillips curve → Empirical finding or theoretically derived from AD-AS model (with AD shocks tracing the curve).

Often assume that  $\pi_t^* = \phi\pi_t^e + (1 - \phi)\pi_{t-1}$ ,

where  $\pi_t^e$  is expected inflation.

$$\pi_t = \phi\pi_t^e + (1 - \phi)\pi_{t-1} + \lambda(\ln Y_t - \ln \bar{Y}_t) + \varepsilon_t^S$$

If Phillips curve → four sources of inflation

- 1) Public expect inflation to be high
- 2) Inflation was high last period (inertia)
- 3) Lack of capacity in economy
- 4) (Supply) shocks, e.g. higher oil prices.

NB: If open economy:

- Assume shocks capture foreign price shocks.
- Add additional term.

Aurelius & Dmitry working on it!

Problemos in steady-state when:

- Output at potential level  $Y_t = \bar{Y}_t$ .

- No shocks

- $\pi_t = \pi_{t-1}$

$\Rightarrow$

- $\pi_t = \pi_t^e!$   $\rightarrow$  What determines  $\pi_t^e$  and/or  $\pi_t$ ?

Before: Seignorage  $\rightarrow$  not relevant for low or moderate inflation levels.

## 10.4 The Dynamic Inconsistency of Low-Inflation Monetary Policy (p. 478)

Nobel Prize territory!

Experiences from 1970s → inflation in 5-15% range > historical average.

General: If short-term trade-off between inflation (surprise) and output ⇒ incentive to inflate to exploit trade-off ⇒ private sector anticipates incentive ⇒ increase inflation expectations ⇒ inflate to avoid output below the natural rate.

DK: The story about the flying prime minister and the “smart” labour union leader!

Kydland & Prescott (1977):

- If discretion → dynamic inconsistency → high inflation!
- One solution → commitment → “tie yourself to the mast” → (binding) rules. [Achilles]
- Other solutions?

Why? Government incentive to inflate, will not carry burden of disinflation

## Model

Lucas supply curve:

$$y = \bar{y} + b(\pi - \pi^e)$$

Government's loss function:

$$L = \frac{1}{2}(y - y^*)^2 + \frac{1}{2}a(\pi - \pi^*)^2, \quad y^* > \bar{y}, a > 0$$

Inflation in discretionary (Nash) equilibrium:

$$\pi^{EQ} = \pi^* + \frac{b}{a}(y^* - \bar{y})$$

Inflationary bias:  $\pi^{EQ} > \pi^*$  and  $y = \bar{y}$ .

... *Whiteboard (3)*

## 10.5 Addressing the Dynamic-Inconsistency Problem (p. 483)

- I) Rules / (binding) commitment.
- II) Reputation.
- III) Delegation.

### I) Rules / (binding) commitment (p. 483)

$$\pi = \pi^* \text{ (binding / commitment)} \Rightarrow \pi^e = \pi^* \Rightarrow y = \bar{y}.$$

→

1. Lower inflation, natural output.
2. Like EE...
3. No/little flexibility.

### II) Reputation (p. 484-487)

Government sets low inflation now / “nice guy” (does not give in for incentive to inflate) to build “reputation”!

Why be nice guy? → Benefit in the future!

- Future surprise / “bad guy” → Mimicking in Perfect Bayesian equilibrium in signalling game.
- Future “good guy” → equilibrium path in Subgame Perfect trigger Equilibrium.

## Reputation in signalling game

Two periods,  $t = 1, 2$

Policymaker's intertemporal objective:

$W = w_1 + \beta w_2$ , where discount factor  $0 < \beta \leq 1$

Two policymaker types, both with inflation target  $\pi^* = 0$ :

Type 1  $\rightarrow$  soft / wet  $\rightarrow$  incentive to inflate:

$$w_t = (y_t - \bar{y}) - \frac{1}{2} a \pi_t^2 = b(\pi_t - \pi_t^e) - \frac{1}{2} a \pi_t^2$$

Type 2  $\rightarrow$  tough / hardnosed  $\rightarrow$  no incentive to inflate:

$$w_t = -\frac{1}{2} a \pi_t^2$$

Private sector's prior probability in period 1 of policymaker being type 1 =  $\Pr(\text{type 1}) = p$ .

Type 2:

$\pi_1 = 0, \pi_2 = 0$  (dominant strategy)

## Type 1:

- Reveal type in period 1 (play  $\pi_1 \neq 0$ )  $\rightarrow$  separating equilibrium.
- Mimic type 2 (play  $\pi_1 = 0$ )  $\rightarrow$  pooling equilibrium.
- Mixed equilibrium...

Period 2  $\rightarrow$  use backward induction:

$$\max_{\pi_2} b(\pi_2 - \pi_2^e) - \frac{1}{2} a \pi_2^2 \Rightarrow \pi_2 = \frac{b}{a}.$$

$$\gg \text{If type 1 reveals type} \Rightarrow \pi_1 = \frac{b}{a}.$$

$$\text{Revelation} \Rightarrow \pi_2^e = \frac{b}{a}.$$

$$W(\pi_1^e | \text{reveal}) = \left[ b \left( \frac{b}{a} - \pi_1^e \right) - \frac{1}{2} a \left( \frac{b}{a} \right)^2 \right] + \beta \left[ 0 - \frac{1}{2} a \left( \frac{b}{a} \right)^2 \right]$$

$\Rightarrow$

$$W(\pi_1^e | \text{reveal}) = -b\pi_1^e + \frac{1}{2} \frac{b^2}{a} (1 - \beta)$$

>> If type 1 mimics type 2  $\Rightarrow \pi_1 = 0$ .

NB: Private sector knows that type 1 (weak) policymaker might “cheat” / mimic strong policymaker!

Label  $q = \Pr(\pi_1 = 0 \mid \text{type 1})$  = probability that a type 1 policymaker mimics.

If  $\pi_1 = 0$  observed:

- Type 2  $\rightarrow$  probability =  $\Pr(\text{type 2}) \cdot \Pr(\pi_1 = 0 \mid \text{type 2}) = (1 - p) \cdot 1 = (1 - p)$ .
- Type 1 mimicking  $\rightarrow$  probability =  $\Pr(\text{type 1}) \cdot \Pr(\pi_1 = 0 \mid \text{type 1}) = pq$ .

Expectation mathematically correct / unbiased  $\rightarrow$  based on Bayes' theorem  $\rightarrow$  Perfect Bayesian equilibrium.

Bayes' theorem:

$$\begin{aligned} \Pr(\text{type 1} \mid \pi_1 = 0) &= \frac{\Pr(\text{type 1}) \cdot \Pr(\pi_1 = 0 \mid \text{type 1})}{\Pr(\pi_1 = 0)} \\ &= \frac{\Pr(\text{type 1}) \cdot \Pr(\pi_1 = 0 \mid \text{type 1})}{\Pr(\text{type 1}) \cdot \Pr(\pi_1 = 0 \mid \text{type 1}) + \Pr(\text{type 2}) \cdot \Pr(\pi_1 = 0 \mid \text{type 2})} \\ &\Rightarrow \end{aligned}$$

$$\Pr(\text{type 1} \mid \pi_1 = 0) = \frac{pq}{pq + (1-p)}$$

$$\pi_2^e \mid_{\pi_1=0} = \mathbb{E}[\pi_2 \mid \pi_1 = 0] = \frac{pq}{pq + (1-p)} \frac{b}{a} + \left(1 - \frac{pq}{pq + (1-p)}\right) 0$$

$\Rightarrow$

$$\pi_2^e \mid_{\pi_1=0} = \mathbb{E}[\pi_2 \mid \pi_1 = 0] = \frac{pq}{pq + (1-p)} \frac{b}{a}$$

$$W(\pi_1^e, q \mid \text{mimic}) = b(0 - \pi_1^e) - \frac{1}{2}a \cdot 0^2 + \beta \left[ b \left( \frac{b}{a} - \frac{pq}{pq + (1-p)} \frac{b}{a} \right) - \frac{1}{2}a \left( \frac{b}{a} \right)^2 \right]$$

$\Rightarrow$

$$W(\pi_1^e, q \mid \text{mimic}) = -b\pi_1^e + \frac{b^2}{a} \beta \left[ \frac{1}{2} - \frac{pq}{pq + (1-p)} \right]$$

(i) If  $q = 0 \rightarrow$  type 1 never mimics. Requires that never favourable to type 1 to mimic:

$$W(\pi_1^e, q = 0 \mid \text{mimic}) \leq W(\pi_1^e \mid \text{reveal})$$

$\Rightarrow$

$$-b\pi_1^e + \frac{b^2}{a}\beta\left[\frac{1}{2} - 0\right] \leq -b\pi_1^e + \frac{1}{2}\frac{b^2}{a}(1-\beta)$$

$$\Rightarrow$$

$$\beta \leq \frac{1}{2}$$

If weak policymaker very impatient, inflate early  $\rightarrow$  no reputation building.

(ii) If  $q = 1 \rightarrow$  type 1 always mimics. Requires that always favourable for type 1 to mimic!

An aside: Calculate posterior when  $q = 1$  and  $\pi_1 = 0$   
 observed:  $\Pr(\text{type 1} \mid \pi_1 = 0) = \frac{p \cdot 1}{p \cdot 1 + (1-p)} = p$ , i.e.  
 private sector learns nothing about policymaker type from observing  $\pi_1 = 0$ .

$$-b\pi_1^e + \frac{b^2}{a}\beta\left[\frac{1}{2} - p\right] \geq -b\pi_1^e + \frac{1}{2}\frac{b^2}{a}(1-\beta)$$

$$\Rightarrow$$

$$\beta \geq \frac{1}{2} \frac{1}{1-p}$$

If very patient  $\Rightarrow$  always mimic  $\rightarrow$  pooling equilibrium!

Patient relative to prior probability of type 1  $\rightarrow$  if high probability of type 1, then little gain from mimicking and surprising in period 2.

(iii) If  $\frac{1}{2} < \beta < \frac{1}{2} \frac{1}{1-p} \Rightarrow$  mixed / randomising strategy supports Perfect Bayesian equilibrium  $\rightarrow$  semi-separating equilibrium! (Choose randomising probability  $0 < q < 1$  so that type 1 indifferent between  $\pi_1 = 0$  and  $\pi_1 = b/a$ .)

Reputation  $\rightarrow$  pooling equilibrium  $\rightarrow$  a weak policymaker builds reputation as tough (hide weakness) and thus sustains low inflation.

“Do not reveal who you really are”  $\rightarrow$  “behave well to avoid consequences if people realise who you really are”!

Repeat many (potentially infinite number of) periods  $\rightarrow$  low inflation reputation sustained for long periods.

### III) Delegation (p. 487-491)

#### Model

$$y = \bar{y} + b(\pi - \pi^e)$$

Government's loss:

$$L = \frac{1}{2}(y - y^*)^2 + \frac{1}{2}a(\pi - \pi^*)^2, \quad y^* > \bar{y}, a > 0$$

Inflation in discretionary equilibrium:

$$\pi^{EQ} = \pi^* + \frac{b}{a}(y^* - \bar{y})$$

Delegate to Central Bank' with  $a'$ :

$$L' = \frac{1}{2}(y - y^*)^2 + \frac{1}{2}a'(\pi - \pi^*)^2$$

Inflation in discretionary equilibrium with delegation:

$$\pi^{EQ'} = \pi^* + \frac{b}{a'}(y^* - \bar{y})$$

$$\pi^e = \pi^{EQ'} \Rightarrow y = \bar{y}.$$

Insert in Government's loss function:

$$L = \frac{1}{2}(\bar{y} - y^*)^2 + \frac{1}{2}a(\pi^* + \frac{b}{a'}(y^* - \bar{y}) - \pi^*)^2$$

$\Rightarrow$

$$L = \frac{1}{2}(\bar{y} - y^*)^2 + \frac{1}{2}a(\frac{b}{a'})^2(y^* - \bar{y})^2$$

Result:  $a' \uparrow \Rightarrow L \downarrow$ .

Society / government better off appointing “conservative Central Banker” with large degree of inflation aversion, i.e.  $a'$  large.

- $a' \rightarrow \infty$  would yield first best.

## **EA: Central-Bank Independence and Inflation (p. 489)**

If III) correct: Countries with “delegation” of monetary policy  $\Rightarrow$  lower inflation, Ceteris Paribus  $\rightarrow$  delegation if CB is “independent” (monetary policy with  $a'$  and not government's  $a$ ).

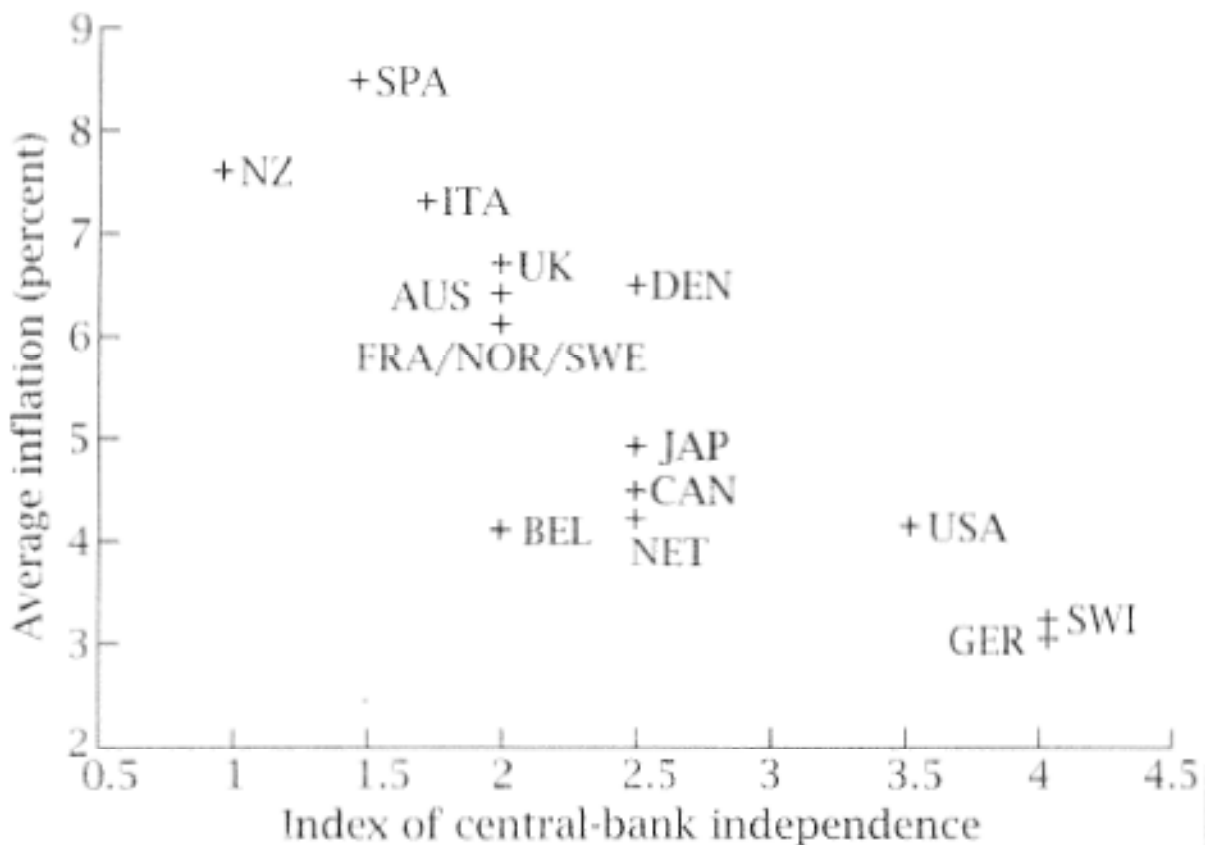


FIGURE 10.6 Central-bank independence and inflation<sup>15</sup>

NB: Causality direction, backward-laying factor like the government's inflation aversion?

Discussion of dynamic inconsistency (p. 491-493)

1. Are forward-looking expectations so important?
2. Inflation affected by variables which are not policy-affected, e.g. oil prices.

## 10.6 What Can Policy Accomplish?

Skip!

## 10.7 The Conduct of Policy

Skip p. 497-499!

Monetary policy increasingly delegated to “independent” or semi-independent central bank.

What do they do? What should they do?

### Interest rate rules (p. 500)

CBs in practice → monetary policy using nominal interest rate:

- Banks’ refinancing facilities → ECB, Norway.
- OMO → USA.

NB: Nominal interest rate rules to avoid instability → react to ensure stability:

- Constant nominal interest rate and  $\pi \uparrow \Rightarrow$  real interest rate  $\downarrow \Rightarrow y \uparrow \Rightarrow \pi \uparrow$ , and so on.

### Taylor (1993)

- FED argues its interest rate setting based on discretionary policies incorporating “ $\infty$ ” variables.
- Taylor:  $i$  setting well described by a rule of form:

$$i_t - \pi_t = \bar{r} + b(\pi_t - \pi^*) + c(\ln Y_t - \ln \bar{Y}_t)$$

where  $\pi^*$  = target inflation,  $\bar{Y}_t$  = natural output at time  $t$ .

Taylor rule!

Taylor (1993) for USA:

$b = 0.5$ ,  $c = 0.5$ ,  $\bar{r} = 2\%$ ,  $\pi^* = 2\%$ ,  $\bar{Y}_t$  = smoothed GDP.

“Issues in the Design...” (p. 501-503) → read yourself!

### Taylor rule used normatively

Is monetary policy expansionary or contractionary?

- Taylor rule indicating “neutral” monetary policy.
- Compare actual real interest rate with real interest rate if Taylor rule followed.

### Monetary Conditions Index

Open economy → changes in real exchange rate ( $e$ ) affect  $Y$  and  $\pi \Rightarrow$  interest rate policy should take this into account.

$$i_t - \pi_t = \bar{r} + b(\pi_t - \pi^*) + c(\ln Y_t - \ln \bar{Y}_t) + de_t$$

where sign of  $d$  depends on definition of  $e$ . (Real appreciation  $e \downarrow \Rightarrow$  real interest rate  $\uparrow$  to retain monetary tightness / same “monetary conditions”.)

$$-de_t + (i_t - \pi_t) = \bar{r} + b(\pi_t - \pi^*) + c(\ln Y_t - \ln \bar{Y}_t)$$

where LHS is the Monetary Conditions Index, i.e.:

$$\text{MCI} = -de_t + (i_t - \pi_t)$$

MCI  $\uparrow \Rightarrow$  tighter / more contractionary monetary conditions.

NB: Sometimes only nominal (and not real) interest rate in MCI.

MCI “intermediate target” in Canada and New Zealand.

## **A Model for Analysing Policy Rules (p. 503)**

Question: What is the loss if CB implements monetary policy as a simple Taylor rule (with inflation and output) even if possible to contingent on many other variables?

Simple model with lags:

$$y_t = -\beta r_{t-1} + \rho y_{t-1} + \varepsilon_t, \quad \beta > 0, 0 < \rho < 1$$

$$\pi_t = \pi_{t-1} + \alpha y_{t-1} + \delta_t, \quad \alpha > 0$$

Shocks  $\varepsilon_t$  and  $\delta_t \rightarrow$  white noise and independent of each other.

After observing  $\varepsilon_t$  and  $\delta_t$ , CB sets  $r_t$  — to minimise the discounted sum of the instantaneous loss:

$$E_t[(y_t - 0)^2] + \lambda E_t[\pi_t^2].$$

 Desired output (normalised)

Interest rule linear in model variables.

NB1: Current  $y_t$  determined by past variables (and shock)  $\Rightarrow$  CB's policy in  $t$  can only affect  $y_{t+1} \Rightarrow$  CB's period  $t$  policy must target  $E[y_{t+1}]$ .

NB2: Inflation in period  $t + 1$  cannot be controlled by period  $t$  policies  $\Rightarrow E[\pi_{t+1}]$  given.

Paths of output and inflation for  $t + 2$  and onwards are, in addition to shocks, determined by  $E[y_{t+1}]$  and  $E[\pi_{t+1}]$ , where  $E[\pi_{t+1}]$  “exogenous”.

Optimal policy  $\sim$  trade-off between  $E[\pi_{t+1}]$  and  $E[y_{t+1}] \Rightarrow$

$$E[y_{t+1}] = -qE[\pi_{t+1}]$$

Can show: Optimal  $q^* = \frac{-\lambda\alpha + \sqrt{\alpha^2\lambda^2 + 4\lambda}}{2}$ .

- If  $\lambda = 0$ , i.e. no inflation concern  $\Rightarrow q^* = 0$ , i.e. expected output back to desired level asap.
- If  $\lambda \rightarrow \infty$ , i.e. no output concern  $\Rightarrow q^* = 1/\alpha$ , i.e. expected inflation back to 0 asap  $\rightarrow$  “inflation combated by recession”.

Optimal policy  $\Rightarrow$

$$r_t = \frac{\rho + q^* \alpha}{\beta} y_t + \frac{q^*}{\beta} \pi_t, \text{ i.e. simple Taylor rule!}$$

NB: Theory suggests (cross) restrictions on parameters in Taylor rule. Satisfied in practice?

## **Inflation Targeting (p. 508)**

Inflation targeting = IT.

IT > CB only targets inflation!

Inflation targeting regime:

- Explicit inflation target.
- Place large weight on inflation target.
- CB's policies transparent and accountable.
- KAR: High degree of CB independence w.r.t. policies.

IT can be optimal policy (if convergence speed to inflation target correct).

### Two views

- Explicit specification of policy regime → credibility, transparency, accountability.
  - Credibility ⇒ disinflation less costly.
- “Conservative window-dressing”. (Change in monetary policy pre-empt change to IT).